

Package: KSD (via r-universe)

September 9, 2024

Type Package

Title Goodness-of-Fit Tests using Kernelized Stein Discrepancy

Version 1.0.1

Date 2021-01-11

Description An adaptation of Kernelized Stein Discrepancy, this package provides a goodness-of-fit test of whether a given i.i.d. sample is drawn from a given distribution. It works for any distribution once its score function (the derivative of log-density) can be provided. This method is based on "A Kernelized Stein Discrepancy for Goodness-of-fit Tests and Model Evaluation" by Liu, Lee, and Jordan, available at [arXiv:1602.03253](https://arxiv.org/abs/1602.03253).

License MIT + file LICENSE

LazyData TRUE

RoxygenNote 7.1.1

Imports pryr, graphics, stats

Suggests datasets, ggplot2, gridExtra, mclust, mvtnorm

Repository <https://minhyung-kang.r-universe.dev>

RemoteUrl <https://github.com/minhyung-kang/ksd>

RemoteRef HEAD

RemoteSha 5d21faf67f60b0c225224f6ac3cc8169952e9c0e

Contents

demo_gmm	2
demo_gmm_multi	2
demo_iris	3
demo_normal_performance	3
demo_simple_gamma	4
demo_simple_gaussian	4
gmm	5

KSD	5
likelihoodgmm	7
perturbgmm	7
plotgmm	8
posteriorgmm	9
rgmm	9
scorefunctiongmm	10

Index	11
--------------	-----------

demo_gmm	<i>Tests 1-dimensional Gaussian Mixture Models.</i>
----------	---

Description

Tests 1-dimensional Gaussian Mixture Models.

Usage

demo_gmm()

demo_gmm_multi	<i>Tests multidimensional Gaussian Mixture Models.</i>
----------------	--

Description

Tests multidimensional Gaussian Mixture Models.

Usage

demo_gmm_multi()

demo_iris	<i>Fits Gaussian Mixture model and computes the KSD value for the model</i>
-----------	---

Description

We fit a Gaussian Mixture Model for a given dataset (Fisher's Iris), and we compute the KSD P-value on the hold-out test dataset. User may tune the parameters and observe the change in results. Reports average of p-values obtained during each k-fold. It also plots the contour for each k-fold iteration if only 2 dimensions of data are used. If a vector is specified for nClust, the code tries each element as the number of clusters and reports the optimal parameter by choosing one with highest p-value.

Usage

```
demo_iris(cols = c(1, 2), nClust = 3, kfold = 5)
```

Arguments

cols	: Columns of iris data set to use. If 2 dimensions, plots the contour for each k-fold.
nClust	: Number of clusters want to estimate with If vector, use each element as number of clusters and reports the optimal number.
kfold	: Number of k to use for k-fold

demo_normal_performance	<i>Shows KSD p value change with respect variation in noise</i>
-------------------------	---

Description

We generate a standard normal distribution, and add varying gaussian noise to this dataset and see the change in pvalues.

Usage

```
demo_normal_performance()
```

demo_simple_gamma *Tests 1-dimensional Gamma Distribution with customized parameters*

Description

We generate a gamma distribution with given parameters, and add gaussian noise to this dataset. We then compute the score of each dataset for the original true distribution.

Usage

```
demo_simple_gamma(
  trueshape = 10,
  truescale = 3,
  noisemu = 5,
  noisesd = 2,
  n = 100
)
```

Arguments

trueshape	shape of true gamma distribution
truescale	scale of true gamma distribution
noisemu	mean of gaussian noise to add
noisesd	standard deviation of gaussian noise to add
n	number of samples to generate

demo_simple_gaussian *Tests 1-dimensional Gaussian Distribution with customized parameters*

Description

We generate a gaussian distribution with given parameters, and add noise to this dataset. We then compute the score of each dataset for the original true distribution.

Usage

```
demo_simple_gaussian(truemu = 5, truesd = 1, noisemu = 0, noisesd = 2, n = 100)
```

Arguments

truemu	mean of true distribution
truesd	standard deviation of true distribution
noisemu	mean of gaussian noise to add
noisesd	standard deviation of gaussian noise to add
n	number of samples to generate

gmm *Returns a Gaussian Mixture Model*

Description

Returns a Gaussian Mixture Model

Usage

```
gmm(nComp = NULL, mu = NULL, sigma = NULL, weights = NULL, d = NULL)
```

Arguments

nComp	(scalar) : number of components
mu	(d by k): mean of each component
sigma	(d by d by k): covariance of each component
weights	(1 by k) : mixing weight of each proportion (optional)
d	: number of dimensions of vector (optional)

Value

model : A Gaussian Mixture Model generated from the given parameters

Examples

```
# Default 1-d gaussian mixture model
model <- gmm()

# 1-d Gaussian mixture model with 3 components
model <- gmm(nComp = 3)

# 3-d Gaussian mixture model with 3 components, with specified mu,sigma and weights
mu <- matrix(c(1,2,3,2,3,4,5,6,7),ncol=3)
sigma <- array(diag(3),c(3,3,3))
model <- gmm(nComp = 3, mu = mu, sigma=sigma, weights = c(0.2,0.4,0.4), d = 3)
```

KSD *Estimate Kernelized Stein Discrepancy (KSD)*

Description

Estimate kernelized Stein discrepancy (KSD) using U-statistics, and use bootstrap to test $H_0: x_i$ is drawn from $p(X)$ (via $KSD=0$).

Usage

```
KSD(x, score_function, kernel = "rbf", width = -1, nboot = 1000)
```

Arguments

x	Sample of size Num_Instance x Num_Dimension
score_function	$(\nabla_x \log p(x))$ Score function : takes x as input and output a column vector of size Num_Instance X Dimension. User may use pryr package to pass in a function that only takes in dataset as parameter, or user may also pass in computed score for a given dataset.
kernel	Type of kernel (default = 'rbf')
width	Bandwidth of the kernel (when width = -1 or 'median', set it to be the median distance between data points)
nboot	Bootstrap sample size

Value

A list which includes the following variables :

- "ksd" : Estimated Kernelized Stein Discrepancy (KSD)
- "p" : p-Value for rejecting the null hypothesis that ksd = 0
- "bootstrapSamples" : the bootstrap sample
- "info": other information, including : bandwidth, M, nboot, ksd_V

Examples

```
# Pass in a dataset generated by Gaussian distribution,
# use pryr package to pass in score function
model <- gmm()
X <- rgmm(model, n=100)
score_function = pryr::partial(scorefunctiongmm, model=model)
result <- KSD(X,score_function=score_function)

# Pass in a dataset generated by Gaussian distribution,
# pass in computed score rather than score function
model <- gmm()
X <- rgmm(model, n=100)
score_function = scorefunctiongmm(model=model, X=X)
result <- KSD(X,score_function=score_function)

# Pass in a dataset generated by Gaussian distribution,
# pass in computed score rather than score function
# Use median_heuristic by specifying width to be -2.0
model <- gmm()
X <- rgmm(model, n=100)
score_function = pryr::partial(scorefunctiongmm, model=model)
result <- KSD(X,score_function=score_function, 'rbf',-2.0)

# Pass in a dataset generated by specific Gaussian distribution,
```

```
# pass in computed score rather than score function
# Use median_heuristic by specifying width to be -2.0
model <- gmm()
X <- rgmm(model, n=100)
score_function = pryr::partial(scorefunctiongmm, model=model)
result <- KSD(X, score_function=score_function, 'rbf', -2.0)
```

likelihoodgmm	<i>Calculates the likelihood for a given dataset for a GMM</i>
---------------	--

Description

Calculates the likelihood for a given dataset for a GMM

Usage

```
likelihoodgmm(model = NULL, X = NULL)
```

Arguments

model : The Gaussian Mixture Model
X (n by d): The dataset of interest, where n is the number of samples and d is the dimension

Value

P (n by k) : The likelihood of each dataset belonging to each of the k component

Examples

```
# compute likelihood for a default 1-d gaussian mixture model
# and dataset generated from it
model <- gmm()
X <- rgmm(model)
p <- likelihoodgmm(model=model, X=X)
```

perturbgmm	<i>Returns a perturbed model of given GMM</i>
------------	---

Description

Returns a perturbed model of given GMM

Usage

```
perturbgmm(model = NULL)
```

Arguments

model : The base Gaussian Mixture Model

Value

perturbedModel : Perturbed model with added noise to the supplied GMM

Examples

```
#Add noise to default 1-d gaussian mixture model
model <- gmm()
noisymodel <- perturbgmm(model)
```

plotgmm

Plots histogram for 1-d GMM given the dataset

Description

Plots histogram for 1-d GMM given the dataset

Usage

```
plotgmm(data, mu = NULL)
```

Arguments

data (n by 1): The dataset of interest, where n is the number of samples.

mu : True mean of the GMM (optional)

Examples

```
# Plot pdf histogram for a given dataset
model <- gmm()
X <- rgmm(model)
plotgmm(data=X)

# Plot pdf histogram for a given dataset, with lines that indicate the mean
model <- gmm()
mu <- model$mu
X <- rgmm(model)
plotgmm(data=X, mu=mu)
```

posteriorgmm	<i>Calculates the posterior probability for a given dataset for a GMM</i>
--------------	---

Description

Calculates the posterior probability for a given dataset for a GMM

Usage

```
posteriorgmm(model = NULL, X = NULL)
```

Arguments

`model` : The Gaussian Mixture Model
`X` (n by d): The dataset of interest, where n is the number of samples and d is the dimension

Value

P (n by k) : The posterior probability of each dataset belonging to each of the k component

Examples

```
# compute posterior probability for a default 1-d gaussian mixture model  
# and dataset generated from it  
model <- gmm()  
X <- rgmm(model)  
p <- posteriorgmm(model=model, X=X)
```

rgmm	<i>Generates dataset from Gaussian Mixture Model</i>
------	--

Description

Generates dataset from Gaussian Mixture Model

Usage

```
rgmm(model = NULL, n = 100)
```

Arguments

`model` : Gaussian Mixture Model defined by gmm()
`n` : number of samples desired

Value

data (n by d): Random dataset generated from given the Gaussian Mixture Model

Note

Requires library mvtnorm

Examples

```
#Generate 100 samples from default gaussian mixture model
model <- gmm()
X <- rgmm(model)

#Generate 300 samples from 3-d gaussian mixture model
model <- gmm(d=3)
X <- rgmm(model,n=300)
```

scorefunctiongmm	<i>Score function for given GMM : calculates score function $d\log p(x)/dx$ for a given Gaussian Mixture Model</i>
------------------	---

Description

Score function for given GMM : calculates score function $d\log p(x)/dx$ for a given Gaussian Mixture Model

Usage

```
scorefunctiongmm(model = NULL, X = NULL)
```

Arguments

model : The Gaussian Mixture Model
X (n by d): The dataset of interest, where n is the number of samples and d is the dimension

Value

y : The score computed by the given function

Examples

```
# Compute score for a given gaussianmixture model and dataset
model <- gmm()
X <- rgmm(model)
score <- scorefunctiongmm(model=model, X=X)
```

Index

demo_gmm, 2
demo_gmm_multi, 2
demo_iris, 3
demo_normal_performance, 3
demo_simple_gamma, 4
demo_simple_gaussian, 4

gmm, 5

KSD, 5

likelihoodgmm, 7

perturbgmm, 7
plotgmm, 8
posteriorgmm, 9

rgmm, 9

scorefunctiongmm, 10